

A Refinement of the Crystal Structure of Potassium Imidodisulphate

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(Received 30 November 1962)

The structure of potassium imidodisulphate, $K_2[NH(SO_3)_2]$, has been refined three-dimensionally in the space-group $C2/c$ by the method of least squares with allowance for anisotropic vibrations and corrections for rotational oscillations. Refinement to a disagreement index of 0.094 over 755 planes has led to the corrected bond lengths $S-N = 1.662 \pm 0.005$ Å and mean $S-O = 1.453 \pm 0.005$ Å, and bond angles $S-N-S = 124.5^\circ$, mean $O-S-O = 113.0^\circ$ and mean $N-S-O = 105.6^\circ$. The hydrogen atom was not explicitly located but is believed to be coplanar with the nitrogen and sulphur atoms. Comparisons are made with the related crystal structures of potassium pyrosulphate and potassium methylenedisulphate.

Introduction

The crystal structure of potassium imidodisulphate or iminodisulphonate (previously called aminedisulphonate), $K_2[NH(SO_3)_2]$, was determined by Jeffrey & Jones (1956) by three-dimensional Fourier methods, ending with an isotropic refinement by two cycles of observed and calculated differential syntheses. From these, the $S-N$ bond was found to have a length 1.655 ± 0.007 Å; Jeffrey & Jones regarded this as a partial double bond as it was intermediate between the $S-N$ lengths of 1.60 ± 0.03 Å in the amidosulphate ion, $[SO_3NH_2]^-$, and 1.79 ± 0.02 Å in the dinitrosulphite ion, $[SO_3N_2O_2]^{2-}$.

Since the structures of the isomorphous crystals of potassium methylenedisulphate, $K_2[CH_2(SO_3)_2]$ (Jones, 1955; Truter, 1962), and potassium pyrosulphate, $K_2S_2O_7$ (Lynton & Truter, 1960), have recently been determined by least-squares methods, with allowance for anisotropic vibrations and rotational-oscillation corrections, it seemed desirable to refine the imidodisulphate data by similar techniques so as to have available dimensions of comparable accuracy for the three isostructural salts. The refinement reported here leads to dimensions differing very little from those reported by Jeffrey & Jones; however, it is possible now to give a fuller description of the crystal structure and of the bonds.

Least-squares refinement

Potassium imidodisulphate crystallizes with the space group $C2/c$ in a unit cell of dimensions

$$a = 12.430, b = 7.458, c = 7.175 \text{ Å}; \beta = 91^\circ 11'.$$

The eight K^+ cations are in general positions and the four $[NH(SO_3)_2]^{2-}$ anions are astride twofold axes

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passing through the nitrogen atoms and possibly through the hydrogen atoms, although the latter were not located by Jeffrey & Jones in an ($F_o - F_c$) synthesis down the $(0, y, \frac{1}{4})$ axis.

The X-ray data used in this refinement were the 687 non-zero $|F_o|$ measured by Jeffrey & Jones together with 68 weak reflexions which were included with values equal to the locally observable minimum $|F_o|$. (As an indication of absorption and estimation errors, measurements from two sets of $\{hkl\}$ photographs taken from different crystals led to a discrepancy index in $|F_o|$ of 0.05 taken over all 64 reflexions recorded.) Five strong reflexions (020, 202, $\bar{2}02$, 400, and 021) were omitted from the least-squares minimization because of presumed extinction, and four others (listed at the end of Table 3) were excluded because of doubts as to their reliability.

Table 1. *Uncorrected monoclinic co-ordinates from least-squares refinements*

Atom	x (Å)	y (Å)	z (Å)
K	4.3201	4.7835	4.6115
S	4.9574	1.3296	4.5903
O(1)	5.5152	2.0264	3.4576
O(2)	4.0792	0.2500	4.2259
O(3)	4.3743	2.2364	5.5416
N	6.2150 ($=a/2$)	0.5745	5.3812 ($=3c/4$)
H	6.2150 ($=a/2$)	-0.4300*	5.3812 ($=3c/4$)

* Assumed.

All the calculations were carried out on the Leeds University Pegasus Computer with programs described by Cruickshank, Pilling, Bujosa, Lovell & Truter (1961). Instead of the Hartree scattering factors with separate isotropic thermal parameters used in the earlier differential syntheses, the scattering factors of Berghuis, Haanappel, Potters, Loopstra, MacGillavry & Veenendaal (1955) for K^+ , O, and N, and a slightly improved version of the curve given by Tomiie & Stam (1958) for S were used in the least-squares refinement. After several cycles in which

Table 2. *Vibration tensor components with respect to crystal axes*
(All values in \AA^2)

Atom	U_{11}	U_{22}	U_{33}	$2U_{12}$	$2U_{23}$	$2U_{13}$
K	0.0403	0.0417	0.0340	0.0008	0.0131	0.0026
S	0.0292	0.0323	0.0270	0.0022	0.0017	0.0043
O(1)	0.0420	0.0600	0.0386	-0.0125	0.0330	0.0039
O(2)	0.0390	0.0455	0.0547	-0.0088	-0.0081	-0.0076
O(3)	0.0440	0.0437	0.0489	0.0257	0.0027	0.0033
N	0.0374	0.0280	0.0332	0	0	0.0133

allowance was made for the anisotropic vibrations of K^+ , S, and O, the R index fell from 0.120 to 0.104. An attempt was then made to locate the hydrogen atoms by carrying out parallel calculations from two sets of atomic positions differing only in the postulated hydrogen sites: (i) a single atom on the two-fold axis, corresponding to coplanarity of the N-H and two N-S bonds; and (ii) a statistical distribution of half hydrogen atoms. In neither case was the hydrogen position confirmed and so this atom was not refined in the full anisotropic refinement, of which nine cycles were carried out. These led to the final atomic co-ordinates shown in Table 1 and the anisotropic vibration parameters shown in Table 2; the largest co-ordinate change from the Jeffrey & Jones values was only 0.018 \AA (in the x co-ordinate of oxygen O(1)). The final values of observed and calculated structure factors are listed in Table 3 and correspond to an R index of 0.094 in which unobserved planes are compared at their maximum possible values. The inclusion of the unobserved reflexions in the least-squares calculations in this way is not entirely satisfactory, but it is unlikely to have affected the results materially. In the later stages of the refinement, the weighting scheme used was

$$w = 1/(4.0 + |F_o| + |F_o|^2/40),$$

where the $|F_o|$'s are on the scale used by Jeffrey & Jones. According to the least-squares refinement, this scale should be increased by a factor 1.064 ± 0.012 .

The co-ordinates' e.s.d.'s determined by the least-squares process are virtually isotropic and have magnitudes 0.0016 \AA for K, 0.0015 \AA for S, 0.006 \AA for O, and 0.008 \AA for the y co-ordinate of N; the e.s.d.'s of the diagonal elements of the mean square vibration amplitudes, U_{ij} , are roughly 0.008 \AA^2 for K and S, 0.0030 \AA^2 for O, and 0.0036 \AA^2 for N.

Molecular vibration analysis

The values of the U_{ij} in Table 2 confirm and elaborate the observation from the earlier differential refinement that the oxygen vibrations are appreciably greater than those of sulphur and nitrogen. Evidently, rotational-oscillation corrections to the co-ordinates of the imidodisulphate ion are needed. Accordingly, the atomic U_{ij} were analysed on the assumption that the ion is undergoing anisotropic rigid-body translations and librations (Cruickshank, 1956). In this ion,

the rigid-body hypothesis is slightly unrealistic in that significant torsional oscillations of the SO_2 groups probably occur about the S-N bonds. Such internal vibrations also necessitate rotational corrections to the co-ordinates (Cruickshank, 1961a). However, as the corrections would be rather similar to those arising from rigid-body librations, no attempt was made to apportion the total angular vibrations between the two kinds.

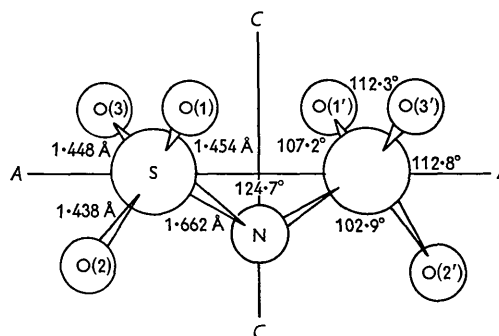


Fig. 1. Rotational axes and corrected dimensions of the imidodisulphate ion.

The molecular vibration analysis was carried out with respect to a set of standard orthogonal axes related to the original monoclinic axes by the co-ordinate transformations:

$$x' = x + z \cos \beta; \quad y' = y; \quad z' = z \sin \beta.$$

In terms of these co-ordinates, the mass centre of the ion is at (6.104, 1.355, 5.380 \AA), which is within 0.025 \AA of the mid-point of the S-S vectors, and the direction cosines of the principal axes of inertia are

A	-0.844,	0.000,	-0.536
B	0.536,	0.000,	-0.844
C	0.000,	1.000,	0.000.

Two of these axes are shown in Fig. 1. A is the axis of minimum inertia ($I_A = 304 \times 10^{-40} \text{ g.cm}^2$) and almost coincides with the S-S' vector; axis B ($I_B = 936$) is perpendicular to the SNS' plane; and axis C ($I_C = 940$) is the twofold-symmetry axis. Within experimental error, the principal axes of both the translational and rotational vibration tensors coincide with the principal axes of inertia. The indicated r.m.s. amplitudes of translational vibration of the ion are 0.18 \AA parallel

Table 3. *Observed and calculated structure factors*
($\times 10$)

In the $|F_o|$ list, entries in brackets are the maximum values for unobserved reflexions
All $|F_o|$ values are 1.064 times those used by Jeffrey & Jones (1956)

h	k	l	$10 F_o $	$10F_c$	h	k	l	$10 F_o $	$10F_c$	h	k	l	$10 F_o $	$10F_c$	h	k	l	$10 F_o $	$10F_c$	
0	0	2	509	-454	7	1	1	447	-444	3	5	1	303	316	4	2	1	168	-143	
0	0	4	934	-832	7	2	2	340	-335	3	5	2	264	-245	4	3	1	489	407	
0	0	6	422	357	7	3	3	(68)	-15	3	5	3	504	456	4	4	1	162	-153	
0	0	8	467	446	7	4	4	(40)	-39	3	5	4	136	-118	4	5	1	231	-210	
0	0	2	180	143	7	5	5	246	262	3	5	5	116	-96	4	6	1	332	319	
0	0	2	939	815	9	1	1	283	286	3	5	6	207	206	4	7	1	45	-53	
0	0	2	94	35	9	2	2	102	-75	3	5	7	33	-36	4	8	1	67	70	
0	0	2	891	-827	9	3	3	145	-117	3	7	0	163	-183	6	1	1	151	176	
0	0	2	374	-345	9	0	0	134	131	3	7	1	318	322	6	2	1	117	103	
0	0	2	(73)	-63	2	0	4	76	70	3	7	2	(52)	13	6	3	1	364	-363	
0	0	2	136	-170	2	0	6	778	-724	3	7	3	162	-145	6	4	1	243	229	
0	0	2	336	335	2	0	8	396	386	3	7	4	198	206	6	5	1	72	-97	
0	0	4	377	-371	2	2	0	373	-423	3	7	5	102	-130	6	6	1	115	-106	
0	0	4	240	-243	2	2	1	938	-1086	3	7	6	162	-166	8	1	1	242	-243	
0	0	4	377	349	2	2	2	780	-760	3	9	0	40	-33	8	2	1	268	186	
0	0	4	3	517	-432	2	2	3	1018	969	3	9	1	218	-220	8	3	1	(53)	10
0	0	4	4	584	556	2	2	4	380	375	3	9	2	126	116	8	4	1	83	-92
0	0	4	5	684	659	2	2	5	380	375	3	1	1	636	-780	1	0	4	41	-35
0	0	4	6	228	-200	2	2	5	364	360	3	1	2	657	726	5	1	1	972	1224
0	0	4	7	105	-86	2	2	7	258	246	3	1	3	159	-180	5	1	2	242	-265
0	0	4	8	129	-148	2	2	8	456	-472	3	1	4	59	-40	5	1	3	73	-63
0	0	6	0	563	562	4	4	0	155	-200	3	1	5	401	387	5	1	4	(46)	-34
0	0	6	1	183	-167	4	4	1	162	171	3	1	6	222	-196	5	1	5	310	-252
0	0	6	2	178	-159	4	4	2	247	239	3	1	7	304	-293	5	1	6	366	351
0	0	6	3	121	109	4	4	3	461	-460	3	1	8	77	-66	5	1	7	183	164
0	0	6	4	454	-499	4	4	4	964	-882	3	1	9	143	-134	5	1	8	76	-76
0	0	6	5	94	83	4	4	5	229	190	3	3	2	622	-703	3	3	0	672	-736
0	0	6	6	162	204	4	4	6	(46)	18	3	3	194	136	5	3	1	343	-346	
0	0	6	7	(50)	19	4	4	7	323	337	3	3	4	168	-156	3	3	2	702	670
0	0	8	0	145	-140	4	4	8	279	290	3	3	5	119	104	5	3	3	367	-339
0	0	8	1	257	264	4	4	9	136	-143	3	3	6	227	209	3	4	4	432	436
0	0	8	2	132	103	6	6	0	105	-113	3	3	7	185	166	5	3	5	133	-116
0	0	8	3	162	135	6	6	1	189	188	3	3	8	51	-51	3	6	6	363	-362
0	0	8	4	(40)	7	6	6	2	572	560	5	5	1	345	346	5	3	7	159	164
0	0	8	5	170	-189	6	6	3	39	-32	5	5	2	513	500	3	0	8	28	-6
1	1	1	223	-266	6	6	4	210	-231	5	5	3	107	97	5	3	0	308	307	
1	1	1	417	-456	6	6	5	65	-78	5	5	4	363	-342	5	5	1	541	-571	
1	1	1	(46)	-5	6	6	6	214	-218	5	5	5	284	-289	5	5	2	91	67	
1	1	1	619	623	6	6	7	107	113	5	5	6	102	-105	5	5	3	248	236	
1	1	1	217	-218	8	8	0	118	-116	5	5	7	105	94	5	5	4	237	-237	
1	1	1	23	19	8	8	1	267	-300	7	7	1	(56)	27	5	5	5	236	256	
1	1	1	68	30	8	8	2	(40)	-8	7	7	2	142	-141	5	5	6	36	33	
1	1	1	189	168	8	8	3	187	180	7	7	3	367	323	5	5	7	115	-69	
1	1	1	94	77	8	8	4	72	78	7	7	4	261	266	5	7	0	72	71	
1	1	1	(60)	-34	8	8	5	59	37	7	7	5	23	41	7	7	1	123	120	
1	1	1	340	-367	0	0	6	698	670	7	7	6	136	-141	7	7	2	258	-259	
1	1	1	33	-26	0	0	8	929	882	7	7	7	41	-40	7	7	3	53	44	
1	1	1	3	305	-321	2	2	1	293	-268	9	9	1	53	-40	7	4	1	125	134
1	1	1	3	186	184	2	2	2	981	1165	9	9	2	128	-120	9	5	0	80	-110
1	1	1	3	313	-310	2	2	3	367	-288	9	9	3	177	-154	9	0	1	103	-114
1	1	1	3	276	-271	2	2	4	1505	-1458	4	4	0	105	-92	9	0	2	(23)	6
1	1	1	3	159	136	2	2	5	247	-208	4	4	0	706	637	9	1	1	250	-276
1	1	1	3	279	-237	2	2	6	126	-120	4	4	0	333	-294	1	1	2	211	241
1	1	1	5	(40)	5	2	2	7	435	-417	4	4	0	335	-265	1	3	2	601	526
1	1	1	5	157	-168	2	2	8	405	421	4	4	2	724	706	1	4	3	615	-477
1	1	1	5	185	197	4	4	1	125	151	4	4	2	232	-268	1	5	4	620	-598
1	1	1	5	474	-451	4	4	2	393	-414	4	4	2	867	-807	1	5	5	620	-598
1	1	1	5	119	-122	4	4	3	729	720	4	4	2	612	-754	1	6	6	(73)	4
1	1	1	5	553	543	4	4	4	654	574	4	4	3	139	-121	1	7	7	248	-246
1	1	1	5	51	-28	4	4	5	294	-258	4	4	4	717	685	3	1	8	159	159
1	1	1	5	43	38	4	4	6	104	97	4	4	5	213	222	3	1	9	57	-91
1	1	1	5	105	109	4	4	7	101	-95	4	4	6	222	213	3	2	0	530	-513
1	1	1	7	117	123	4	4	8	290	-293	4	4	7	(56)	30	3	3	530	-513	
1	1	1	7	160	143	6	6	1	202	211	4	4	8	134	180	3	4	1	331	295
1	1	1	7	366	-319	6	6	2	107	97	4	4	1	401	433	3	5	2	600	548
1	1	1	7	250	-243	6	6	3	581	-544	4	4	2	454	480	3	6	3	167	158
1	1	1	7	(33)	12	6	6	4	(60)	5	4	4	85	95	3	7	4	117	103	
1	1	1	7	60	-53	6	6	5	58	48	4	4	3	76	79	3	6	5	72	-62
1	1	1	9	189	158	6	6	6	63	-82	4	4	4	532	-546	3	8	6	264	-304
1	1	1	9	112	98	6	6	7	248	263	4	4	5	579	-587	5	1	7	110	-103
1	1	1	9	78	74	8	8	1	132	-117	4	4	6	80	63	5	2	8	327	-325
1	1	1	9	214	176	8	8	2	148	145	4	4	7	51	35	5	3	500	-533	
1	1	1	9	503	-627	8	8	3	108	108	4	4	8	105	144	5	4	4	169	-159
1	1	1	9	89	115	8	8	4	148	145	4	4	0	553	-575	5	5	5	23	20
1	1	1	9	148	-157	6	6	5	108	115	4	6	0	137	133	5	6	6	112	134
1	1	1	9	237	224	6	6	6	139	-183	4	6	1	212	210	5	7	7	152	166
1	1	1	9	137	158	6	6	7	76	82	4	6	2	180	179	5	8	8	305	313
1	1	1	9	197	207	6	6	8	83	-68	4	6	3	253	268	7	1	9	218	214
1	1	1	9	123	115	6	6	9	331	-407	4	6	4	51	48	7	2	0	102	92
1	1	1	9	125	-115	6	6	10	631	697	4	6	5	148	-126	7	3	1	80	-96
1	1	1	9	316	383	6	6	11	453	413	4	6	6	81	85	9	1	2	102	-136
1	1	1	9	348	330	6	6	12	279	-299	4	8	0	189	-192	9	0	3	714	711
1	1	1	9	134	-144	6	6	13	93	92	4	8	1	241	-227	9	0	4	1071	-1065
1	1	1	9																	

Table 3 (cont.)

			$10 F_o $	$10 F_c$				$10 F_o $	$10 F_c$				$10 F_o $	$10 F_c$				$10 F_o $	$10 F_c$
<i>h</i>	<i>k</i>	<i>l</i>			<i>h</i>	<i>k</i>	<i>l</i>			<i>h</i>	<i>k</i>	<i>l</i>			<i>h</i>	<i>k</i>	<i>l</i>		
6	4	3	332	353	7	7	3	171	-139	5	5	2	57	-53	12	6	0	85	69
4	4	4	(35)	9	7	7	4	69	-79	5	5	3	546	420	12	6	1	155	-161
4	4	5	-1	0	0	0	0	164	135	5	5	4	51	64	12	6	2	98	105
4	4	6	272	-295	0	0	2	344	-315	5	5	5	216	-231	12	0	2	239	-228
4	4	7	214	-248	0	0	4	113	-89	7	7	1	(34)	-12	12	0	4	211	-178
6	6	0	74	-65	0	0	6	(66)	-17	7	7	2	125	-118	12	0	6	(36)	9
6	6	1	243	-265	2	2	0	83	-94	7	7	3	161	-125	12	2	1	208	221
6	6	2	180	-178	2	2	1	(39)	31	7	7	4	104	-123	12	2	2	210	208
6	6	3	(60)	117	2	2	2	444	433	10	0	0	256	-220	12	2	3	89	101
6	6	4	117	142	2	2	3	169	173	10	0	2	214	-188	12	2	4	(32)	14
6	6	5	222	259	2	2	4	209	214	10	0	4	156	-152	12	2	5	72	-120
6	6	6	138	165	2	2	5	143	-147	10	2	0	48	42	12	4	1	129	-135
6	6	8	209	200	2	2	6	(62)	-30	10	2	2	87	36	12	4	2	129	-128
6	6	8	109	121	2	2	7	(52)	-24	10	2	3	104	-111	12	4	3	(36)	45
6	6	8	33	23	4	4	0	252	-279	10	2	4	172	-126	12	4	4	99	70
6	6	8	88	-81	4	4	1	239	-255	10	2	5	42	32	12	6	1	127	133
0	0	2	351	320	4	4	2	266	-267	10	2	6	(52)	-30	12	6	2	48	-50
0	0	4	179	-159	4	4	3	87	-79	10	4	0	86	-72	13	1	0	189	187
0	0	6	541	-479	4	4	4	151	145	10	4	1	98	-104	13	1	1	268	267
0	0	8	274	243	4	4	5	256	271	10	4	2	85	-74	13	1	2	220	-204
2	2	1	267	-261	4	4	6	36	52	10	4	3	70	-71	13	1	3	98	-91
2	2	2	58	-75	4	4	7	84	-111	10	4	4	162	-220	13	1	4	185	-156
2	2	3	637	589	6	6	0	140	141	10	4	5	84	90	13	3	0	380	-293
2	2	4	223	-205	6	6	1	134	118	10	4	6	58	70	13	3	1	343	-339
2	2	5	31	-19	6	6	2	41	-54	10	6	0	75	73	13	3	2	109	119
2	2	6	127	136	6	6	3	265	-246	10	6	1	222	262	13	3	2	261	260
2	2	7	205	-272	6	6	4	(48)	-51	10	6	2	(41)	38	13	3	3	125	103
2	2	8	38	-41	6	6	5	64	-78	10	6	3	116	58	13	3	4	67	86
4	4	1	652	-742	8	8	0	86	-83	10	0	2	98	73	13	5	0	60	63
4	4	2	252	-247	8	8	1	(33)	-29	10	0	4	122	-102	13	5	1	257	-255
4	4	3	257	-220	8	8	2	261	277	10	0	6	72	-65	13	5	2	190	-190
4	4	4	274	-228	0	0	2	583	-551	10	2	1	(56)	14	13	1	1	63	42
4	4	5	(40)	258	0	0	4	295	-244	10	2	2	88	94	13	1	2	159	151
4	4	6	(41)	-27	0	0	6	77	56	10	2	3	60	-61	13	1	3	538	441
4	4	7	85	78	0	0	8	67	82	10	2	4	348	353	13	1	4	160	-168
6	6	1	274	-282	2	2	1	276	294	10	2	5	102	116	13	3	1	125	-148
6	6	2	314	301	2	2	2	195	-193	10	2	6	(49)	-46	13	3	2	(43)	13
6	6	3	94	-96	2	2	3	102	-94	10	2	7	33	-55	13	3	3	103	-96
6	6	4	50	-64	2	2	4	259	249	10	4	1	262	-276	13	3	4	50	-33
6	6	5	129	136	2	2	5	136	-136	10	4	2	77	-58	13	3	5	278	277
6	6	6	(42)	-144	2	2	6	85	95	10	4	3	105	-92	13	5	1	107	-104
8	8	1	157	-144	2	2	7	(48)	-26	10	4	4	169	-168	14	0	2	77	81
8	8	2	33	-24	4	4	1	145	128	10	4	5	136	146	14	0	3	51	-36
8	8	3	174	-160	4	4	2	165	155	10	4	6	65	62	14	0	4	267	223
8	8	4	198	-206	4	4	3	367	-315	10	4	7	65	62	14	0	5	117	90
1	1	0	290	334	4	4	4	118	-85	10	6	1	245	248	14	2	0	(46)	25
1	1	1	77	-90	4	4	5	(33)	36	10	6	2	94	81	14	2	1	194	-207
1	1	2	84	75	4	4	6	118	-114	10	6	3	(53)	53	14	2	2	89	-97
1	1	3	1023	968	4	4	7	98	120	11	1	0	365	-388	14	4	0	145	138
1	1	4	492	-495	6	6	0	189	-206	11	1	1	(56)	-46	14	4	1	197	217
1	1	5	340	-318	6	6	1	103	95	11	1	2	156	-154	14	4	2	83	-86
1	1	6	60	-14	6	6	2	217	181	11	1	3	627	-627	14	0	2	451	-371
1	1	7	223	-257	6	6	3	92	-106	11	1	4	235	255	14	0	4	197	198
1	1	8	170	185	6	6	4	37	43	11	1	5	159	137	14	2	1	125	131
3	3	0	698	-718	8	8	0	198	-206	11	3	0	152	119	14	2	2	56	57
3	3	1	169	168	8	8	1	312	-339	11	3	1	390	375	14	2	3	265	-213
3	3	2	402	-430	1	1	0	633	-778	11	3	2	46	-13	14	2	4	94	-102
3	3	3	36	-13	1	1	1	473	505	11	3	3	329	318	14	4	1	(33)	36
3	3	4	440	450	1	1	2	112	122	11	3	4	43	20	14	4	2	121	111
3	3	5	163	-140	1	1	3	70	83	11	3	5	37	-21	15	1	0	115	99
3	3	6	195	203	1	1	4	387	385	11	3	6	56	-81	15	1	1	33	-29
3	3	7	41	-12	1	1	5	335	-288	11	5	0	187	-186	15	1	2	157	147
3	3	8	69	68	1	1	6	223	-192	11	5	1	125	-128	15	1	3	(244)	192
5	5	0	17	-17	3	3	0	742	-779	11	5	2	(23)	-14	15	3	0	130	-144
5	5	1	29	-25	3	3	1	144	-155	11	5	3	305	264	15	3	1	71	-80
5	5	2	357	-353	3	3	2	436	-435	11	5	4	103	105	15	3	2	214	253
5	5	3	(27)	-23	3	3	3	173	177	11	5	5	419	-487	15	3	3	145	-99
5	5	4	97	87	3	3	4	240	-266	11	5	6	274	292	15	3	4	40	-4
5	5	5	160	-152	3	3	5	90	80	11	5	7	223	219	15	3	5	36	-37
5	5	6	211	212	3	3	6	346	369	11	5	8	(35)	10	15	3	2	119	161
5	5	7	94	-104	3	3	7	(33)	11	11	1	1	266	324	16	0	0	290	-243
5	5	8	86	86	5	5	0	157	-163	11	5	9	174	-164	15	1	1		
5	5	9	203	183	5	5	1	409	462	11	5	10	148	-151	0	2	0	973	-1148
7	7	3	107	-146	5	5	2	80	74	11	5	11	553	-551	0	2	1	1233	1420
1	1	1	405	462	5	5	3	51	-44	11	5	12	(46)	44	0	2	2	1714	2204
1	1	2	327	-321	5	5	4	33	45	11	5	13	107	-92	2	2	0	1597	-1874
1	1	3	310	-317	5	5	5	281	-270	11	5	14	23	-29	4	0	0	1336	-1886
1	1	4	100	-102	5	5	6	46	-41	11	5	15	314	371	4	4	6	38	110
1	1	5	627	-656	7	7	1	163	-176	11	5	16	310	336	11	7	5	136	-242
1	1	6	315	327	7	7	2	127	123	11	5	17	46	48	10	6	4	19	-85
1	1	7	262	284	7	7	3	103	74	11	5	18	150	-143	11	3	4	240	-282
3	3	1	(47)	-56	1	1	1	82	-91	12	0	0	49	51					
3	3	2	165	176	1	1	2	154	-144	12	0	1	350	324					
3	3	3	917	1013	1	1	3	706	-720	12	0	2	(52)	32					
3	3	4	198	192	1	1	4	288	210	12	0	3	192	-163					
3	3	5	233	209</															

Table 4. Observed and calculated vibration tensor components with respect to inertial axes

(All values in Å²)

Atom	U_{11}		U_{22}		U_{33}		U_{12}		U_{13}		U_{23}	
	obs.	calc.	obs.	calc.	obs.	calc.	obs.	calc.	obs.	calc.	obs.	calc.
S	0.0300	0.0310	0.0262	0.0269	0.0323	0.0321	0.0003	0.0001	-0.0014	0.0002	0.0001	-0.0001
O(1)	0.0420	0.0391	0.0385	0.0345	0.0600	0.0615	0.0010	0.0072	-0.0033	-0.0058	0.0175	0.0133
O(2)	0.0392	0.0364	0.0547	0.0576	0.0455	0.0471	-0.0049	-0.0030	0.0058	0.0113	-0.0011	-0.0012
O(3)	0.0460	0.0392	0.0469	0.0377	0.0437	0.0451	-0.0025	-0.0072	-0.0116	-0.0043	-0.0057	-0.0120
N	0.0414	0.0337	0.0289	0.0271	0.0280	0.0227	-0.0008	-0.0007	0	0	0	0

to A , 0.14 Å parallel to B , and 0.15 Å parallel to C ; the apparent r.m.s. angular oscillations are 6.8° about A , 3.7° about B , and 3.9° about C . Thus the axis associated with the largest oscillations is that with the minimum inertia and the least cross-section. The same effect was found in the $K_2S_2O_7$ and $K_2[CH_2(SO_3)_2]$ structures, though in the former the apparent translation vibrations were rather smaller than in the present structure. This difference is probably due to a slight systematic error in one or other set of experimental data, most likely the neglect of absorption corrections for the pyrosulphate. However, this possible systematic error is not important

Table 5. Monoclinic co-ordinates of the anion after rotational correction

Atom	x (Å)	y (Å)	z (Å)
S	4.9530	1.3294	4.5864
O(1)	5.5151	2.0314	3.4460
O(2)	4.0725	0.2418	4.2215
O(3)	4.3665	2.2432	5.5455
N	6.2150 ($=a/2$)	0.5677	5.3812 ($=3c/4$)
H	6.2150 ($=a/2$)	-0.4400	5.3812 ($=3c/4$)

for the present purpose, since the chief aim of the vibration analysis is to obtain the rotational corrections for the co-ordinates. The U_{ij} calculated with the above translational and librational rigid-body vibrations together with the observed U_{ij} with respect to the inertial axes are shown in Table 4; there is an r.m.s. difference of 0.0040 Å² between the observed and calculated values. Since this is not much greater than the 0.0030 Å² estimated earlier for the oxygen U_{ii} e.s.d.'s, the rigid-body hypothesis evidently accounts for the major part of the anisotropic vibrations, and the derived librational amplitudes may justifiably be used to calculate the rotational corrections for the co-ordinates. Table 5 gives the revised co-ordinates; the largest correction is 0.012 Å to the z co-ordinate of O(1).

Discussion

Table 6 gives the bond lengths and angles obtained from both the uncorrected and corrected co-ordinates. (See Fig. 1 for the numbering of the atoms.) The corrected dimensions differ by at most 0.009 Å and 0.8° from those given by Jeffrey & Jones, whose work is thus satisfyingly corroborated by the present more detailed refinement. From the co-ordinate e.s.d.'s

given above, the e.s.d.'s in the individual dimensions are calculated as S-O 0.006 Å, S-N 0.004 Å, \angle O-S-O and \angle N-S-O 0.3°, \angle S-N-S 0.5°. The three S-O bond lengths are equal within experimental error and their mean is 0.006 Å greater than the Jeffrey & Jones mean, chiefly because of the rotational corrections. The e.s.d. of the mean is roughly $0.006/\sqrt{3}=0.004$ Å, but to allow for the effects of some neglected off-diagonal terms in the least-squares matrix and for any inaccuracies in the rotational corrections, it would be

Table 6. Molecular dimensions

	Jeffrey & Jones	Present uncorrected	Rotationally corrected
S-N	1.655 Å	1.654 Å	1.662 Å
S-O(1)	1.454	1.451	1.461
S-O(2)	1.438	1.434	1.442
S-O(3)	1.448	1.446	1.457
Mean S-O	1.447	1.444	1.453
S-N-S	124.7°	125.7°	125.5°
O(1)-S-O(2)	113.5	114.0	114.0
O(2)-S-O(3)	112.8	112.7	112.8
O(3)-S-O(1)	112.3	112.3	112.3
N-S-O(1)	107.2	107.0	107.0
N-S-O(2)	102.9	103.5	103.2
N-S-O(3)	106.9	106.5	106.5

Corrected intramolecular distances between non-bonded atoms:

O(1)-O(2)	2.44 Å	O(2)-O(3)	2.41 Å	O(3)-O(1)	2.42 Å
N-O(1)	2.51	N-O(2)	2.44	N-O(3)	2.50
O(1)-O(3')	3.08	S-S'	2.96		

prudent to increase the e.s.d.'s of S-O (mean) and S-N from 0.004 to 0.005 Å. The mean S-O length is therefore 1.453 ± 0.005 Å and S-N is 1.662 ± 0.005 Å. The variations among the individual O-S-O angles and among the O-S-N angles are just outside experimental error and presumably are due to steric effects. The mean O-S-O angle is 113.0° and the mean O-S-N angle is 105.6°. The revised values for the shorter intramolecular distances between non-bonded atoms are shown also in Table 6; there are no important differences from the values given by Jeffrey & Jones.

Jeffrey & Jones reported that they had been unable to locate the hydrogen electron density unequivocally by difference synthesis, and that the planar configuration, rather than a statistical pyramidal one, about the nitrogen atom could be inferred only from the S-N bond lengths. We have been no more successful

with the least-squares technique, as the inclusion of the hydrogen atom, whether on the axis or in a statistical distribution of half-atoms off the axis, gave no improvement to the residual and led to implausible parameter shifts for the atom. Siebert (1957) reports a single infra-red frequency centred on 3235 cm^{-1} for the NH stretching vibration, but it is rather broad and thus leaves the nature of the H sites in doubt. However, in the electron spin resonance spectrum of an irradiated potassium imidodisulphate crystal, Horsfield, Morton, Rowlands & Whiffen (1962) detected at certain orientations a small splitting of the ^{14}N triplet in the trapped $\cdot\text{N}(\text{SO}_3)_2^-$ radical; this is attributed to interactions with hydrogen nuclei in the host imidodisulphate ions. On the whole, the e.s.r. line shape tends to favour the existence of a single hydrogen site in the normal molecule.

In his theoretical discussion of π -bonds involving the $d_{x^2-y^2}$ and d_{z^2} orbitals of sulphur, Cruickshank (1961*b*) has carried considerably further the interpretation of the dimensions of the imidodisulphate ion given by Jeffrey & Jones. Here, we remark only that the S-N bond of $1.662 \pm 0.005\text{ \AA}$ is of a similar length to the S-O(4) (bridge) bond of $1.645 \pm 0.005\text{ \AA}$ in the pyrosulphate ion (Lynton & Truter, 1960). On Cruickshank's theory, they are both partial double bonds in contrast to the appreciably larger S-C bond of $1.770 \pm 0.007\text{ \AA}$ in the methylenedisulphate (Truter, 1962), which cannot easily acquire any double-bond character since the carbon is bonded to four other atoms.

The slight differences of about 0.2 \AA in the cell dimensions of the isostructural compounds $\text{K}_2\text{S}_2\text{O}_7$, $\text{K}_2[\text{NH}(\text{SO}_3)_2]$, and $\text{K}_2[\text{CH}_2(\text{SO}_3)_2]$ may be attributed partly to the extra space required for the hydrogen atom in the imidodisulphate and for the two hydrogen atoms in the methylenedisulphate. A second cause is that the intra-ionic dimensions of the common parts of the anions also differ by as much as 0.1 \AA .

Table 7. *The shorter* $\text{K} \cdots \text{O}$ *interatomic distances*
(All values in \AA)

$\text{K} \cdots \text{O}(1)$	3.23(I)	2.75(II)	2.83(V)
$\text{K} \cdots \text{O}(2)$	2.95(I')	3.00(III)	3.05(VIII)
$\text{K} \cdots \text{O}(3)$	2.71(I)	2.70(II)	2.82(VIII)

These distances refer to the cation K(I), and the roman numerals are those on the anions in Fig. 2(a).

In each crystal structure, the principal interionic contacts are between potassium and oxygen atoms; for potassium imidodisulphate, the revised $\text{K} \cdots \text{O}$ distances are given in Table 7. In all three structures, these sets of $\text{K} \cdots \text{O}$ contacts are very similar. On the other hand, there are important differences in the way contacts are made with the bridging groups: O(4), NH, and CH_2 . For convenience, Jeffrey & Jones's illustrations of the $\text{K}_2[\text{NH}(\text{SO}_3)_2]$ structure are reproduced as Fig. 2; the corresponding illustrations of the other two structures would be sufficiently similar.

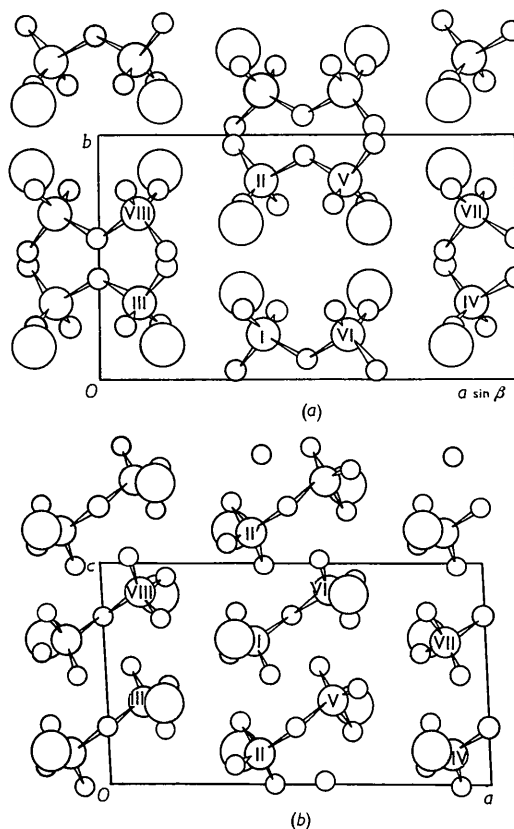


Fig. 2. Crystal structure of $\text{K}_2[\text{NH}(\text{SO}_3)_2]$ projected (a) down $[001]$ and (b) along $[010]$.

In the pyrosulphate, the bridge atom O(4) is not involved in any electrostatic or interionic van der Waals contacts, as the O(4) of group I/VI is 3.31 \AA from the O(1)'s and 3.36 \AA from the O(2)'s of the groups II' and V. [See Fig. 2(b).] In the imidodisulphate, though the nitrogen is at similar distances 3.17 and 3.41 \AA , from the O(1)'s and O(2)'s, the hydrogen (assumed coplanar with the nitrogen and sulphur atoms) is only 2.41 \AA from the two O(1)'s; this distance is appropriate to a van der Waals contact. In the methylenedisulphate, the hydrogens are no longer on the twofold axis and each is close to an O(1) (2.54 \AA), an O(2) (2.43 \AA), an S (2.74 \AA) and an H (2.34 \AA) of the adjacent group (the carbon is 3.47 \AA from two O(1)'s and 3.39 \AA from two O(2)'s).

While most of the interionic $\text{O} \cdots \text{O}$ distances in this structure are in excess of 3.2 \AA , there is in each structure one interionic $\text{O} \cdots \text{O}$ separation which is only slightly longer than a van der Waals distance. This is the contact from O(3) of I to O(2) of VIII; the distances are 3.04 , 3.00 , and 3.13 \AA in the three salts of pyrosulphate, imidodisulphate, and methylenedisulphate respectively.

We thank Dr A. Horsfield for early communication of his electron spin resonance measurements, our

colleagues for the use of programs, and the Leeds University Computing Laboratory for facilities.

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The Crystal Structure of Trimethyloxosulfonium Fluoborate $[(\text{CH}_3)_3\text{SO}]^+\text{BF}_4^-$

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(Received 8 August 1962)

Crystals of $[(\text{CH}_3)_3\text{SO}]^+\text{BF}_4^-$ are orthorhombic with unit cell dimensions

$$a = 11.49 \pm 0.01, b = 11.80 \pm 0.01, c = 11.58 \pm 0.01 \text{ \AA}.$$

The space group is *Pbcn* with $Z = 8$. Although the $[(\text{CH}_3)_3\text{SO}]^+$ ion is not required crystallographically to have any symmetry, it approximates closely to symmetry $3m$. The fluoborate ions are crystallographically of two types and both are required to have the symmetry 2. However, these ions achieve this symmetry in a statistical (disordered) manner.

Bond distances and angles in the trimethyloxosulfonium ion are: S-C(1) = 1.77 ± 0.02 \AA, S-C(2) = 1.78 ± 0.02 \AA, S-C(3) = 1.78 ± 0.02 \AA, S-O = 1.45 ± 0.01 \AA, C(1)-S-C(2) = $106.8 \pm 0.8^\circ$, C(1)-S-C(3) = $107.2 \pm 0.8^\circ$, C(2)-S-C(3) = $105.1 \pm 0.8^\circ$, C(1)-S-O = $112.6 \pm 0.7^\circ$, C(2)-S-O = $112.1 \pm 0.7^\circ$, C(3)-S-O = $112.7 \pm 0.7^\circ$.

Because of the disorder, it was not possible to obtain accurate bond distances and angles in the fluoborate ions.

Introduction

The crystal structure of trimethyloxosulfonium perchlorate has been reported by Coulter, Gantzel & McCullough (1961, 1963). At the time it became apparent that the perchlorate is disordered, the study of the fluoborate salt was undertaken with the hope that it would be ordered and thus permit a more accurate determination of the distances and angles in the $(\text{CH}_3)_3\text{SO}^+$ ion. Although it was found that the fluoborate salt was even more disordered than the perchlorate, the distances and angles in the $(\text{CH}_3)_3\text{SO}^+$ ion are in excellent agreement with the values found in the perchlorate and the structure reported for this interesting ion in the previous paper is confirmed.

Experimental

The preparation of trimethyloxosulfonium fluoborate has been described by Smith (1959) who kindly supplied the analyzed sample used in this study.

Crystals suitable for the X-ray work were grown by the slow evaporation of solutions of the salt in acetone, in which it is only slightly soluble.

Weissenberg and precession photographs about the *c* axis of the unit appear much like those of the perchlorate. However, on closer inspection it was apparent that the fluoborate has orthorhombic rather than tetragonal symmetry. The lattice constants are:

$$a = 11.49 \pm 0.01, b = 11.80 \pm 0.01, c = 11.58 \pm 0.01 \text{ \AA}$$

based on $\text{Cu } K\alpha = 1.5418$ \AA. The only systematic absences are $0kl$ with k odd, $h0l$ with l odd and $h+k$ odd. The space group was accordingly assumed to be *Pbcn*. The flotation density of the crystals was found to be 1.52 g.cm^{-3} while that calculated for $Z = 8$ is 1.523 g.cm^{-3} .

The intensity data were obtained from sets of multiple-film Weissenberg photographs about the *b* and *c* axes prepared with $\text{Cu } K\alpha$ radiation. The crystals were about 0.18 mm by 0.20 mm in cross-section and the corresponding value of μR for copper radia-